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Inflation and Welfare in Long-Run Equilibrium with Firm Dynamics

We analyze the welfare cost of inflation in a model with a cash-in-advance constraint and an endogenous distribution of establishments' productivities. Inflation distorts aggregate productivity through firm entry dynamics. The model is calibrated to the U.S. economy and the long-run equilibrium properties are compared at low and high inflation. When the period over which the cash-in-advance constraint is binding is one quarter, an annual inflation rate of 10% leads to a decrease in average productivity of roughly 0.5% compared to the optimum. This decrease is not innocuous: it leads to a doubling of the welfare cost of inflation.

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WHETHER THE ADOPTION OF monetary policy rules that reduce inflation and interest rates leads to important welfare gains is a central question in monetary economics (Lucas 2000). Calculations often suggest that the effects of changes in the inflation rate on capital accumulation are modest. However, if international differences in income per capita are explained by differences in the accumulation of productive factors and by differences in the efficiency in the employment of these factors, then the welfare cost of inflation will be high if it discourages the

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accumulation of factors of production or if it leads to less efficiency in their use.¹ The first possibility has been extensively examined in the literature; however, the latter has been neglected. In this paper we begin the exploration of this second possibility.

In an influential paper, Cooley and Hansen (1989) provide estimates of the welfare costs of inflation within the framework of a neoclassical monetary economy where money is held because of a cash-in-advance (CIA) constraint. At moderate inflation rates, these models produce relatively modest welfare costs; for example, Cooley and Hansen (1989) report that, in steady state, a 10% inflation rate results in a welfare cost of about 0.5% of steady-state consumption relative to an optimal monetary policy.

However, in these earlier models average productivity is exogenous and only the accumulation of factors of production matters to determine income. Gomme (1993), De Gregorio (1993), and Jones and Manuelli (1995) extend the work on the effects of monetary policy to models of endogenous growth and find the welfare cost of inflation to be either of the same magnitude or an order of magnitude smaller. But their work assumes a single representative firm and abstracts from heterogeneity in production units. If, however, the allocation of aggregate resources across uses is important in understanding cross-country differences in per capita incomes, then it is not only the level of factor accumulation that matters but also how these factors are allocated across heterogeneous production units.²

In this paper, we investigate what is the impact of higher rates of monetary growth on the economy in a model where the productivity distribution of incumbent establishments is endogenous. For this purpose, we consider establishment heterogeneity along the lines of Hopenhayn (1992), Hopenhayn and Rogerson (1993), and Melitz (2003) to explain the endogenous selection of firms in the industry. We incorporate this framework into a monetary economy characterized with a CIA constraint on consumption and investment goods, and in addition we assume that the liquidity constraint also applies to the creation of new establishments. Thus, in the model individuals must use cash to create new business start-ups. This assumption is supported by substantial evidence that finance constraints are often binding constraints facing aspiring entrepreneurs.

For instance, in work using U.S. micro data, Evans and Leighton (1989) and Evans and Jovanovic (1989) have argued formally that entrepreneurs face liquidity constraints. Blanchflower and Oswald (1998) present further evidence on the barriers to entrepreneurship, this time based on the National Survey of the Self-Employed, which draws on information from a random sample of approximately 12,000 adults interviewed in Britain in the spring of 1987. Individuals who were recently

^{1.} Indeed, the prevailing view in development accounting is that cross-country differences in income per capita are mostly explained by differences in Total Factor Productivity (see King and Levine 1994, Klenow and Rodriguez-Clare 1997, Prescott 1998, Hall and Jones 1999, Caselli 2005).

^{2.} There is substantial evidence of the importance of capital and labor allocation across establishments as a determinant of aggregate productivity. Studies document that about half of overall productivity growth in U.S. manufacturing can be attributed to factor reallocation from low- to high-productivity establishments for different time periods (see, e.g., Baily, Hulten, and Campbell 1992, Bartelsman and Doms 2000, Foster, Haltiwanger, and Syverson 2008, among others).

self-employed were asked to name the main source of finance used to set up their business. Out of the 243 respondents who were in this special category, 42% reported that they used their own savings to set up the business, 15% used money from family or friends, while only 17% took a bank loan. When asked the question "What help would have been most useful to you in setting up your business?" the most commonly recorded item—by the same group of individuals—was assistance with money and finance (mentioned by a quarter of respondents).³ All this evidence is consistent with a binding CIA constraint for business start-ups and suggests that whatever goods or services need to be purchased to create new businesses, they are difficult to purchase through credit.⁴

Our framework allows us to analyze the effect of long-run monetary growth on average productivity. In addition to discouraging investment and labor supply, we find that an increase in the long-run rate of money growth increases the cost of creating new establishments. As the cost of creating new establishments increases, there is less industry entry and the number of incumbent establishments' falls. This in turn leads to lower wages and allows establishments with low productivity to stay in the industry leading to a reallocation of the factors of production toward less efficient establishments. The adjustment in the size distribution of incumbents lowers the economy's average productivity.

We calibrate the model to the U.S. economy and find that an annual inflation rate of 10% leads to a decrease in the steady-state average productivity of about 0.5%, compared to the efficient steady state. Furthermore, we estimate the welfare cost due to the inflation tax of 10% inflation to be about 0.9% of aggregate consumption, using a quarter for the period over which money must be held. As it turns out, roughly half of the welfare cost of inflation is associated with the fall in average productivity. We consider several alternative calibrations to the benchmark economy, revealing the importance of the assumptions made regarding the returns to scale and the dispersion of productivities across establishments.

We also provide an alternative measure of the welfare cost of not implementing the optimal monetary policy that takes into account the transition path after the implementation of the policy reform. When the transition dynamics are considered the welfare cost is lower since it takes time for consumption to increase to the new steady state and agents spend more time working along the transition path. However, when the CIA constraint applies to the creation of new firms the welfare cost of inflation is still substantial even considering the whole transition path. Moreover,

^{3.} Blanchflower and Oswald (1998) provide another elucidating test of the finance-constraint hypothesis. The test uses data on inheritances and gifts and their results show that individuals who have received money through inheritances or gifts are more likely to run their own businesses. This finding suggests that some sort of CIA constraint is a binding constraint on the creation of new businesses. Similar evidence is reported in Holtz-Eakin, Joulfaian, and Rosen (1994).

^{4.} The World Bank Doing Business annual surveys measure several barriers to entry which an entrepreneur must overcome to start a new business. Most countries have a minimum capital requirement, i.e., the amount that the entrepreneur needs to deposit in a bank or with a notary before registration and up to 3 months following incorporation. This again provides evidence in favor of a CIA constraint hampering business start-ups. We thank an anonymous referee for pointing out this.

when we take into account the transition path, roughly 85% of the welfare cost of inflation is associated with the low average productivity at high rates of inflation.

In work which is related to this paper, Wu and Zhang (2001) examine the effects of anticipated inflation in a framework characterized by monopolistic competition and a well-defined industry structure. In their paper, firms' mark-ups are affected by the rate of inflation. They find that at higher rates of inflation firms are fewer and smaller in size. The resulting welfare cost of inflation is larger than the conventional estimates. In our paper, the welfare cost of inflation is also higher than those obtained in conventional models. Moreover, as their model, our model also predicts that the number of incumbent establishments is lower at high rates of inflation. However, in our paper markets are competitive and the higher welfare cost is associated with the change in the productivity distribution of incumbent establishments.

Given the abundance of empirical evidence indicating the importance of producers' heterogeneity and selection-based productivity growth, it is hardly surprising that an influential literature has developed which examines the reallocation effects of policy distortions. In the article mentioned earlier, Hopenhayn and Rogerson (1993) consider the effect on average productivity and welfare of employment protection in a setting characterized with firm entry and exit dynamics. They find that a tax on job destruction results in a decrease in average productivity of over 2%. In a related paper Veracierto (2001) extends Hopenhayn and Rogerson's analysis of firing taxes by introducing a flexible form of capital and considering transition dynamics. Veracierto finds that firing taxes equal to one year of wages have large long-run effects: they decrease steady-state output, capital, consumption, and wages by 7.84% and steady-state employment by 6.62%. With the purpose of studying the role of international trade, Melitz (2003) shows how aggregate industry productivity growth caused by reallocations across heterogeneous establishments contributes to additional welfare gains from trade liberalization.

The role of policy distortions in environments with industry dynamics has also influenced the literature on development. For instance, Restuccia and Rogerson (2008) consider policy distortions that lead to reallocation of resources across heterogeneous firms. Their aim is to examine whether policies that leave aggregate relative prices unchanged but distort the prices faced by different producers can explain crosscountry differences in per capita incomes. In their benchmark model they find that the reallocation of resources implied by such policies can lead to decreases in output and productivity in the range of 30% to 50%, even though the underlying range of available technologies across establishments is the same in all policy configurations. Samaniego (2006) proposes a model of plant dynamics to analyze the effects of policies that affect establishments differently depending on the stage of their life-cycle, notably subsidies to failing plants. He finds that these subsidies may increase aggregate productivity. Guner, Ventura, and Xu (2008) find that policies that distort the size distribution of incumbent establishments may lead to a substantial reduction in output and productivity.

Finally, our paper also relates to an emerging and growing body of research that studies whether variation in distortions to the allocation of resources across firms caused by variation in entry barriers are a major determinant of cross-country income differences. Work by Barseghyan and DiCecio (2010) has shown that the observed variation in regulatory entry costs leads to substantial cross-country differences in TFP and output. This happens because entry barriers allow unproductive firms to operate, changing the industry composition and lowering its average productivity. Poschke (2010) tries to explain differences in aggregate productivity between similar industrialized countries such as the U.S. and European Union member states with shifts in administrative entry cost in a model of heterogeneous firms close to Hopenhayn (1992). Alfaro, Charlton, and Kanczuk (2008) investigate, using plant-level data for several countries, whether differences in the allocation of resources across heterogeneous plants are a significant determinant of cross-country differences in income per worker. They find that allowing for firm heterogeneity improves the model ability to explain differences in productivity across countries. Our paper introduces firm heterogeneity and industry dynamics into a monetary growth model and considers the distortions introduced by the inflation tax, when money holdings are required to create new establishments.

The remainder of the paper is organized as follows. In Section 1 we lay out the details of our model and describe the stationary competitive equilibrium. In Section 2 we investigate the qualitative effect of changes in the monetary growth rate on the endogenous real aggregates and the size distribution of productive establishments. Section 3 discusses the procedure for calibrating our model and Section 4 presents our model-based quantitative findings and also examines the robustness of our findings to changes in the economic environment. Finally, Section 5 concludes.

1. THE MODEL

We consider a CIA production economy, which exhibits establishment level heterogeneity as studied by Hopenhayn (1992) and Hopenhayn and Rogerson (1993). Establishments have access to a decreasing returns to scale technology, pay a fixed cost to remain in operation each period and are subject to entry and exit. In what follows we first describe the problem of the household confronted with a CIA constraint; next we describe the production side in more detail and finally characterize the stationary competitive equilibrium.

1.1 The Household

There is an infinitely lived representative household with preferences over streams of consumption and leisure at each date described by the utility function

$$\sum_{t=0}^{\infty} \beta^t \left(\ln C_t + A \ln L_t \right),$$

where C_t is consumption at date t, L_t is leisure and $\beta \in (0, 1)$ is the discount factor.⁵ The representative agent is endowed with one unit of productive time each period. She owns three types of assets: capital, cash, and production establishments. The period 0 endowment of each asset is strictly positive.

The timing of the household decision problem resembles the one in Stockman (1981). The household enters period t with nominal money balances equal to m_{t-1} that are carried over from the previous period and in addition receives a lump-sum transfer equal to gM_{t-1} (in nominal terms), where M_t is the per capita money supply in period t. Thus, the money stock follows the law of motion

$$M_t = (1+g) M_{t-1}.$$

Output can (i) be used as a consumption good, (ii) be used as an investment good which increases the stock of capital owned by the household, or (iii) be purchased to create new establishments constituting an entry cost. Households are required to use their previously acquired money balances to purchase goods. Because we want to compare situations when the constraint applies to some types of good but not to others, we introduce three parameters that we denote by θ_i with i = c, k, h. When $\theta_c = 1$ the CIA constraint applies to the consumption good, when $\theta_k = 1$ purchases of the investment good are constrained and when $\theta_h = 1$ the constraint applies to the entry cost needed to create a new establishment. When $\theta_i = 0$ (i = c, k, h) the constraint does not apply to the specific good. Hence, the constraint reads as

$$\theta_c C_t + \theta_k X_t + \theta_h \kappa E_t \le \frac{m_{t-1} + g M_{t-1}}{p_t},\tag{1}$$

where p_t is the price level at time t, κ is the quantity of goods that has to be purchased to create each new establishment, E_t is the mass of new establishments created and X_t is investment, given by

$$X_t = K_{t+1} - (1 - \delta) K_t,$$
(2)

where K_t is the capital stock.

The representative household must choose consumption, investment, leisure, nominal money holdings, and the mass of new establishments subject to the CIA constraint (1) and the budget constraint

$$C_t + X_t + \kappa E_t + \frac{m_t}{p_t} \le w_t N_t + r_t K_t + \xi_t \bar{z}_t H_t + (m_{t-1} + g M_{t-1}) / p_t, \quad (3)$$

where $N_t \equiv (1 - L_t)$ is time spent working, H_t is the mass of (incumbent) establishments, and ξ_t is the fraction of incumbent establishments that choose to be productive

^{5.} The log –log specification for preferences is a popular choice in the real business cycle literature (see Cooley and Prescott 1995). It implies a Frisch elasticity of labor supply equal to one, which is in the middle range of the usual estimates. See Chetty et al. (Forthcoming) for a recent discussion of the empirical evidence. However, our findings are not very sensitive to changes in the value of the Frisch elasticity.

at time t (determined endogenously as explained below); also, w_t is the wage rate, r_t is the rate of return on capital and \bar{z}_t are average dividends across productive incumbent establishments.

We assume that the gross growth rate of money (1 + g) always exceeds the discount factor β , which is a sufficient condition for (1) to always bind in equilibrium and existence of a stationary equilibrium.⁶ We sometimes denote real money balances by $\mu_t \equiv m_t/p_t$.

1.2 Production Establishments

Once a new establishment is created at t, its idiosyncratic productivity $s \in S$ is revealed as drawn from a distribution F(s) and remains constant over time until the establishment exits the industry. At t + 1 the establishment starts production. Incumbent establishments produce output by renting labor and capital. The production function of an establishment with idiosyncratic productivity s at time t is

$$y_{s,t} = sn_{s,t}^{\alpha}k_{s,t}^{\nu} - \eta, \tag{4}$$

where $n_{s,t}$ and $k_{s,t}$ are labor and capital employed, η is a fixed operating cost, $\alpha \in (0, 1)$, $\nu \in (0, 1)$, and $\nu + \alpha < 1$. The flow profits of an incumbent establishment are given by

$$z_{s,t} = \max_{n_{s,t},k_{s,t}} \{ s n_{s,t}^{\alpha} k_{s,t}^{\nu} - w_t n_{s,t} - r_t k_{s,t} - \eta \},$$
(5)

where w_t is the wage rate and r_t is the return on capital.

Incumbent establishments exit when hit by an exogenous shock. In particular, in any given period after production takes place each establishment faces a constant probability of death equal to λ . Moreover, incumbent establishments face an endogenous period-by-period decision over whether to produce or not. Incumbent establishments that choose to produce incur a fixed operating cost. However, in any period, an incumbent may stay in the industry but choosing not to produce. In such a case the establishment survives but does not incur the fixed operating cost and earns zero profits that period.⁷ Consequently, incumbent establishments choose not to produce when

$$z_{s,t} < 0.$$

We denote by s_t^* the idiosyncratic productivity threshold below which establishments choose to exit. Specifically, s_t^* is such that $z_{s_t^*,t} = 0$. The fraction of incumbent establishments that choose to become productive in period *t* is $\xi_t = 1 - F(s_t^*)$.

^{6.} It can be shown that the existence of a steady state requires $1 + g \ge \beta$ (see Abel 1985).

^{7.} This assumption allows us to study the transition dynamics of the model analytically (see Chaney 2005, Bilbiie, Ghironi, and Melitz 2007).

Given the first-order conditions which solve the problem of incumbent firms (5) the labor demand by an establishment with productivity s is

$$n_{s,t} = s^{\sigma} \left(\frac{\alpha}{w_t}\right)^{(1-\nu)\sigma} \left(\frac{\nu}{r_t}\right)^{\nu\sigma}$$
(6)

and the demand for capital reads

$$k_{s,t} = s^{\sigma} \left(\frac{\alpha}{w_t}\right)^{\alpha\sigma} \left(\frac{\nu}{r_t}\right)^{(1-\alpha)\sigma},\tag{7}$$

where $\sigma = (1 - \alpha - \nu)^{-1}$. Replacing the factor demands into the profit function yields

$$z_{s,t} = \Omega \frac{s^{\sigma}}{w_t^{\alpha\sigma} r_t^{\nu\sigma}} - \eta, \tag{8}$$

where $\Omega = \alpha^{\alpha\sigma} \nu^{\nu\sigma} - \alpha^{(1-\nu)\sigma} \nu^{\nu\sigma} - \alpha^{\alpha\sigma} \nu^{(1-\alpha)\sigma}$.

Let h(s; t) denote the mass of incumbent establishments with productivity level *s* at time *t*. The motion equation for h(s; t) is given by

$$h(s;t+1) = (1-\lambda)h(s;t) + E_t \frac{dF(s)}{ds},$$
(9)

with $H_t = \int_{s \in S} h(s; t) ds$ denoting the mass of incumbent establishments. Consequently, the mass of entrants reads

$$E_t = H_{t+1} - (1 - \lambda) H_t.$$
(10)

1.3 Market Clearing

Market-clearing conditions for labor and capital are given, respectively, by

$$N_t = \int_{s \ge s_t^*} n_{s,t} h(s;t) \, ds \tag{11}$$

and

$$K_t = \int_{s \ge s_t^*} k_{s,t} h(s;t) \, ds. \tag{12}$$

Market clearing in the money market requires

$$m_t = M_t. \tag{13}$$

Finally, the economy's feasibility constraint reads

$$C_t + X_t + \kappa E_t = Y_t, \tag{14}$$

where $Y_t \equiv \int_{s \ge s_t^*} y_{s,t} h(s;t) \, ds$.

1.4 Stationary Equilibrium

The Bellman equation characterizing household's optimal behavior reads as

$$V(m_{t-1}, K_t, H_t) = \max_{C_t, L_t, m_t, K_{t+1}, H_{t+1}} \{\ln C_t + A \ln L_t + \beta V(m_t, K_{t+1}, H_{t+1})\},$$
(15)

and is subject to the CIA constraint (1) and the budget constraint (3), together with equations (2) and (10). We begin by considering the steady-state competitive equilibrium of the model. In a steady-state equilibrium the productivity threshold s^* , the rental rates, and all the real aggregates are constant over time. Moreover, the gross rate of inflation $\Pi \equiv p_{t+1}/p_t$ is constant too, equal to the gross rate of monetary growth 1 + g. Thus, we henceforth ignore all time subscripts to simplify the notation. Following Melitz (2003), it is useful to define average productivity as

$$\bar{s} = \left\{ \int_{s \ge s^{\star}} s^{\sigma} \frac{dF(s)}{1 - F(s^{\star})} \right\}^{\frac{1}{\sigma}}.$$
(16)

Hence, with the knowledge of s^* one can identify average productivity \bar{s} . From equation (8) this implies that average dividends read as

$$\bar{z} = \int_{s \ge s^{\star}} z_s \frac{dF(s)}{1 - F(s^{\star})} \, ds = \Omega \frac{\bar{s}^{\sigma}}{w^{\alpha \sigma} r^{\nu \sigma}} - \eta. \tag{17}$$

We now illustrate three effects of inflation related to the CIA constraint. Consumption and leisure in the steady-state equilibrium satisfy the condition

$$\frac{L}{C} = \frac{A}{w} \left[1 + \theta_c \left(\frac{1+g}{\beta} - 1 \right) \right].$$
(18)

Equation (18) suggests that when the CIA constraint applies to consumption, an increase in inflation raises the cost of consumption relative to leisure. This result corresponds to the effect examined in Cooley and Hansen (1989).

The representative household problem yields the stationary equilibrium rental rate of capital, given by

$$r = \left(\frac{1}{\beta} - 1 + \delta\right) \left[1 + \theta_k \left(\frac{1+g}{\beta} - 1\right)\right].$$
(19)

Equation (19) shows that the rental cost of capital is increasing in the rate of anticipated inflation when the CIA constraint applies to the investment good. It also suggests the following mechanism. When the CIA constraint applies to investment, inflation increases the cost of holding money balances, which reduces capital accumulation. As a result, at higher inflation, the rental cost of capital is higher. This result is due to Stockman (1981).

Finally, the establishment's free-entry condition reads

$$\kappa \left[1 + \theta_h \left(\frac{1+g}{\beta} - 1 \right) \right] = \left[1 - F(s^*) \right] \frac{\beta \bar{z}}{1 - \beta (1-\lambda)}.$$
(20)

Equation (20) states that in equilibrium the sunk cost that has to be paid to create a new establishment (the left-hand side of (20)) has to be equal to the expected discounted profits from creating this establishment (the right-hand side of (20)). The rate of discount of profits depends on the household discount factor β and the probability λ that the new establishment dies in future periods. The probability $[1 - F(s^*)]$ also appears on the right-hand side of (20) because one has to account for the probability of successful entry when evaluating discounted profits.

Equation (20) characterizes the mechanism by which money growth affects the establishments entry decision. When the CIA constraint applies to the entry cost, an increase in inflation makes entry more costly. The next section shows that this has an effect on average productivity too.

Hence, inflation may have three effects, depending on the structure of the CIA constraint. It may affect labor supply, capital accumulation, and the productivity distribution of incumbent establishments. Each effect contributes to lowering the level of output. This allows us, in the next section, to state a proposition on the real effects of inflation. Before doing this, we go through the remaining relationships characterizing the equilibrium.

In the stationary competitive equilibrium the optimal exit rule by incumbent establishments requires $z_{s^{\star}} = 0$. This yields a solution for the productivity threshold, given by

$$s^{\star} = w^{\alpha} r^{\nu} \left(\frac{\eta}{\Omega}\right)^{1-\alpha-\nu}.$$
(21)

Since the equilibrium interest rate is determined by (19), the exit condition characterizes a relationship between the wage rate and the productivity threshold which is represented by the *SS* locus in Figure 1.

In turn, the expected value of entry—i.e., the right-hand side of the free-entry condition (20)—is locally independent of s^* by the envelope theorem (see Appendix A.1 for proof). Consequently, the equilibrium wage rate is independent of s^* , as illustrated by the *WW* locus in Figure 1. Hence, in an equilibrium with production the free-entry condition determines the wage rate.

Finally, the motion equations for capital and for the number of incumbent firms respectively, equations (2) and (10)—together with the resource constraint (14) complete the characterization of the stationary competitive equilibrium. The stationary competitive equilibrium is defined as follows:⁸

^{8.} It is shown in Appendix A.2 that the equilibrium exists and is unique.



FIG. 1. Determination of s^* and w in the Stationary Economy.

DEFINITION 1. A stationary competitive equilibrium is a wage rate, w, a rental rate of capital, r, an aggregate distribution of establishments, h(s), a mass of entry, E, a household value function, V(m, K, H), an establishment profit function, z_s , a productivity threshold, s^* , policy functions for incumbent establishments, n_s and k_s , and aggregate levels of consumption, C, employment, N, capital, K and real money balances, μ , such that:

- (i) The household optimizes: equations (15), (18), (19), and (20);
- (ii) Establishments optimize: equations (6), (7), (8), and (21);
- (iii) Markets clear: equations (11), (12), (13), and (14);
- (iv) h(s) is an invariant distribution—i.e., a fixed point of (9).

To summarize, the model is solved as follows. First, the rental cost of capital is pinned down by equation (19). Then, given the value of r, one can solve for the values of the wage rate w and the productivity threshold s^* from (20) and (21). One can consequently characterize fully the stationary distribution of capital, employment, profits, and output with equations (4), (6), (7), and (8) across incumbent firms. Finally, the feasibility constraint (14) together with the other market-clearing conditions and the first-order condition for leisure (18) allow to determine the mass of incumbents H and all the aggregates of the economy such as investment, consumption, output, the stock of capital, and employment.⁹

^{9.} In Appendix B.1 (available from the authors' website), we present all the equations that characterize the stationary equilibrium for the particular restriction that we impose on the distribution F. See also Section 4 where we describe the calibration procedure.

2. THE REAL EFFECTS OF INFLATION

We now investigate the relationship between inflation, the equilibrium aggregates K and N, and the size distribution of productive establishments, characterized by s^* . Proposition 1 summarizes our main results.

PROPOSITION 1. Consider the stationary competitive equilibrium as defined earlier.

- (i) If $\theta_c = 1$ and $\theta_k = \theta_h = 0$, an increase in the inflation rate Π is associated with a fall in the equilibrium capital stock K and a fall in the employment rate N. However, the productivity threshold s^{*} does not change.
- (ii) If $\theta_k = 1$ and $\theta_c = \theta_h = 0$, an increase in the inflation rate Π is associated with a fall in the equilibrium capital stock K and a fall in the employment rate N. However, the productivity threshold s^{*} does not change.
- (iii) If $\theta_h = 1$ and $\theta_c = \theta_k = 0$, an increase in the inflation rate Π is associated with a fall in the equilibrium capital stock K, a fall in the employment rate N, and a fall in the productivity threshold s^* .

In what follows, we discuss some aspects related to Proposition 1. The detailed proof is developed in Appendix A.3.

When consumption is subject to the CIA constraint condition (18) is affected by money growth. At high rates of inflation, the marginal utility of leisure must fall with respect to the product of the wage rate and the marginal utility of consumption, leading the household to supply less labor. Fewer hours worked leads to lower output and therefore lower consumption and capital stock. The rental cost of capital, determined by (19), remains the same and, therefore both the SS curve and the WW curve, in Figure 1, are unaffected. Thus the wage rate and average productivity are unaffected.

Figures 2 and 3 illustrate items (ii) and (iii) of Proposition 1. When $\theta_k = 1$ —i.e., investment is subject to the CIA constraint—condition (19) is affected. At high rates of inflation the return on capital must increase as individuals are less willing to invest. Because labor and capital are complementary in the production function, labor demand decreases and the wage rate falls. Moreover, the probability of successful entry must remain unchanged in equilibrium since the cost of creating a new establishment (the left-hand side of equation (20)) has not changed. This is illustrated in Figure 2.

When the entry cost is subject to the CIA constraint, $\theta_h = 1$, the cost of creating new establishments is affected by the monetary growth rate. Therefore, the comparative statics is the same as the one corresponding to an increase in the entry cost, illustrated in Figure 3. In particular, consider the comparative statics of moving from a stationary equilibrium with a low rate of monetary growth to an equilibrium with a high rate of monetary growth. At high rates of monetary growth the cost of creating new establishments is high. Therefore, fewer establishments are created. With less industry entry the number of incumbent firms falls and consequently there is less demand for labor. Therefore, the wage rate falls. Accordingly the WW locus has to shift to the



FIG. 2. Effect of an Increase in g on s^* and w When $\theta_k = 1$ and $\theta_c = \theta_k = 0$.



Fig. 3. Effect of an Increase in g on s^* and w When $\theta_h = 1$ and $\theta_c = \theta_h = 0$.

left which translates into a movement along the SS curve: with lower wage rates, low productivity establishments decide to produce output. This in turn leads to a lower productivity threshold.

3. CALIBRATION

In this section, we describe the model calibration procedure. Since we consider alternative configurations for the CIA constraint—corresponding to different values for θ_i , i = c, k, h—the calibration of some parameters changes across specification. When this happens, we report the values taken by the parameters for each specification (see Table 1).

Notation	Parameter	Value
g	Monetary growth rate	0.0060
α	Labor income share	0.6400
ν	Capital income share	0.2100
δ	Depreciation rate of capital	0.0160
β	Household's discount factor	
	Model specifications for which:	
	$\theta_k = 0$	0.9902
	$\theta_k = 1$	0.9906
ε	Pareto distribution shape parameter	7.2655
λ	Failure rate of incumbent establishments	0.0179
<i>s</i> ₀	Pareto distribution lower bound	1.0000
κ	Sunk entry cost	1.0000
η	Fixed operating cost	
	Model specifications for which:	
	$\theta_k = 1 \text{ and } \theta_h = 1$	0.9063
	$\theta_k = 0$ and $\theta_h = 1$	0.9035
	$\theta_k = 1$ and $\theta_h = 0$	0.9092
	$\theta_k = 0$ and $\theta_h = 0$	0.9065
Α	Disutility of labor	
	Model specifications for which:	
	$\theta_c = 1 \ \theta_k = 1 \ \text{and} \ \theta_h = 1$	2.3939
	$\theta_c = 1 \theta_k = 0$ and $\theta_h = 1$	2.3889
	$\theta_{c} = 0 \theta_{k} = 1$ and $\theta_{h} = 1$	2.4311
	$\theta_c = 0 \theta_k = 0$ and $\theta_h = 1$	2.4270
	$\theta_c = 1 \ \theta_k = 1 \ \text{and} \ \theta_h = 0$	2.3982
	$\theta_c = 1 \ \theta_k = 0 \text{ and } \theta_h = 0$	2.3932
	$\theta_c = 0 \ \theta_k = 1 \ \text{and} \ \theta_h = 0$	2.4354
	$\theta_c = 0 \ \theta_k = 0 \text{ and } \theta_h = 0$	2.4314

TABLE 1	

PARAMETERS: SUMMARY

Notes: The calibration of β , η , and A varies according to the model specification and, in particular, according to the value taken by θ_c , θ_k , and θ_c . Thus, we report the values taken by the parameters β , η , and A, for each specification.

To solve our model we need to specify a distribution for the establishments' productivity draws F(s). Following Helpman, Melitz, and Yeaple (2004), we assume a Pareto distribution for F with lower bound s_0 and shape parameter $\varepsilon > \sigma$, i.e., $F(s) = 1 - (s_0/s)^{\varepsilon}$. The shape parameter is an index of the dispersion of productivity draws: dispersion decreases as ε increases, and the productivity draws are increasingly concentrated toward the lower bound s_0 . This assumption has two advantages: it generates a distribution of idiosyncratic productivities among incumbent establishments that fits microeconomic data quite well (see Axtell 2001, Cabral and Mata 2003) and delivers closed-form solutions for the endogenous aggregates.¹⁰ Specifically, the distribution of productivities among incumbent establishments, which is the distribution F left-truncated at s^* , is also Pareto with lower bound s^* and shape parameter ε .

10. See Appendix B.1 (available from the authors' website) for a complete description of the model solution.

Parameter values are selected so that the steady state of the model economy reproduces several important features of U.S. data. Furthermore, we assume that the length of time that the CIA constraint is binding is one quarter and calibrate the model accordingly. The growth rate of the money supply g is chosen to be 0.006, corresponding to an annual rate of inflation of 2.43%. This choice matches the average annual rate of inflation in the U.S. between 1988 and 2007, reported in the World Economic Indicators.

For the labor and capital income shares, α and ν , respectively, empirical evidence concerning establishment level returns to scale reported by Atkeson and Kehoe (2005) suggests the relationship $\alpha + \nu = 0.85$. In particular, these authors consider this choice to be consistent with the evidence in Atkeson, Khan, and Ohanian (1996). The separate identification of α and ν is done by setting the labor income share to be 64%, $\alpha = 0.64$, as is standard in the real business cycle literature.

The depreciation rate is chosen on the basis of estimated depreciation by the Bureau of Economic Analysis (BEA). Thus, we set $\delta = 0.0160$, implying an annual depreciation rate of 6.54%. Given the depreciation rate, the rental cost of capital *r* is chosen so that the annual real interest rate is 4%. The implied value for the rental cost of capital is r = 0.03. In turn, this implies $\beta = 0.9906$ when investment is subject to the CIA constraint—i.e., $\theta_k = 1$ —and $\beta = 0.9902$ when it is not—i.e., $\theta_k = 0$.

The parameter measuring the disutility of labor A is chosen so that individuals spend 25.5% of their endowment of time working. This is based on Gomme and Rupert (2007) who interpret evidence from the American Time-Use Survey. Depending on the model specification, this yields a value for A ranging between 2.3889 and 2.4354.

Following Ghironi and Melitz (2005), we choose the shape parameter of the productivity draws' distribution to match the standard deviation of log U.S. plant sales (which in our case is also output). This is reported to be 1.67 in Bernard et al. (2003). In our model the standard deviation is $1/(\varepsilon - \sigma)$, implying that the value for ε is 7.2655. The establishments death rate λ is chosen based on empirical evidence reported in Dunne, Roberts, and Samuelson (1989). These authors perform an empirical investigation of establishment turnover using data on plants that first began operating in the 1967, 1972, or 1977 Census of Manufacturers, a rich source of information concerning the U.S. manufacturing sector. They report 5-year exit rates among plants aged 1–5 year old (39.7%), 6–11 year old (30.3%), and older (25.5%). As expected, plant failure rates decline with age. We choose to calibrate the exit rate of incumbent establishments by matching the exit rate of 6- to 11-year-old firms. This yields a value for λ of 0.0179, implying that each quarter 1.79% of incumbent establishments exit the industry.

The remaining parameters to be calibrated are s^0 , η , and κ . Notice first that s_0 can be normalized to 1 without loss of generality because it has no impact on the endogenous exit decision of new establishments. Moreover, only the ratio η/κ is identifiable. Therefore, we normalize the sunk cost κ to 1 and solve for the resulting fixed operating cost η . The statistic used to determine η is the establishments' average employment. In particular, Hopenhayn and Rogerson (1993), using data from the Manufacturing Establishments Longitudinal Research Panel, report the average number of employees

CALIBRATION: TARGETS

Target	Value
U.S. average annual inflation rate (1988–2007)	0.0243
Production function returns to scale	0.85
Labor income share	0.64
Annual real interest rate	0.04
Annual depreciation rate of capital	0.0654
Standard deviation of log U.S. plant sales	1.67
Manufacturing establishments (6–10 years old) failure rates	0.303
Average establishment size (number of employees)	62
Fraction of time spent working (rate)	0.255

Notes: The parameters s_0 and κ are normalized to 1.

in manufacturing establishments to be about 62 employees. Since, as reported above, individuals spend 25.5% of their endowment of time working, this implies that the average establishment employment in units of time is 15.81. The resulting value of the fixed operating cost η ranges between 0.9035 and 0.9092, depending on the model specification.¹¹

This completes the calibration description. Table 1 summarizes the parameter values and Table 2 the targets informing our choices.

4. RESULTS

The Friedman rule—i.e., deflating at the rate of time preference—is optimal in this economy.¹² We use the model economy just described to contrast the efficient steady state to the long-run equilibria associated with alternative monetary policy rules. In particular, we describe how the macroeconomic aggregates, including output, consumption, investment, and aggregate hours as well as the number of incumbent establishments and average productivity vary with respect to the Pareto optimal allocation, at various rates of monetary growth. We then use the model to measure the welfare costs of anticipated inflation under alternative model specifications. Later, we examine the role played by firm heterogeneity and the level of returns to scale in explaining our findings. Finally, we examine how our conclusion about the welfare cost of inflation is affected once we consider the transition path between alternative steady states.

^{11.} The implied value for the entry-to-operating cost ratio is 1.09. This value is close to the value proposed in an analogous framework by Barseghyan and DiCecio (2010). They calibrate the entry-to-operating costs to 0.82 basing their choice on evidence from the recent IO empirical literature. For instance, Aguirregabria and Mira (2007) and Dunne et al. (2009) in studies covering different industries propose estimates for the entry-to-operating cost that are concentrated around 1.

^{12.} We show this is the case in Appendix A.5.

Annual inflation rate in %	$\begin{array}{c} 100 \times \\ (\beta^4 - 1) \end{array}$	0.00	2.43 ^a	10.00	15.00	$\begin{array}{c} 100 \times \\ (\beta^4 - 1) \end{array}$	0.00	2.43 ^a	10.00	15.00
	Ра	anel A: 6	$\theta_c = 1$ as	nd $\theta_k =$	1	Pa	nel B: 6	$P_c = 1$ and	nd $\theta_k =$	0
Output	100.00	98.60	97.71	95.14	93.56	100.00	98.98	98.36	96.55	95.43
Consumption	100.00	98.87	98.15	96.04	94.74	100.00	99.09	98.54	96.92	95.91
Investment	100.00	97.67	96.22	92.03	89.50	100.00	98.98	98.36	96.55	95.43
Hours	100.00	99.10	98.54	96.87	95.84	100.00	99.19	98.70	97.25	96.35
No. of establishments	100.00	98.60	97.71	95.14	93.56	100.00	98.98	98.36	96.55	95.43
Productivity	100.00	99.87	99.79	99.54	99.39	100.00	99.87	99.78	99.54	99.39
	Pa	anel C: 6	$\theta_c = 0$ and	nd $\theta_k =$	1	Pa	nel D: 6	$\theta_c = 0$ as	nd $\theta_k =$	0
Output	100.00	99.29	98.84	97.52	96.71	100.00	99.71	99.53	99.00	98.67
Consumption	100.00	99.56	99.28	98.45	97.93	100.00	99.82	99.71	99.38	99.17
Investment	100.00	98.36	97.33	94.33	92.52	100.00	99.71	99.53	99.00	98.67
Hours	100.00	99.80	99.67	99.30	99.07	100.00	99.92	99.87	99.72	99.63
No. of establishments	100.00	99.29	98.84	97.52	96.71	100.00	99.71	99.53	99.00	98.67
Productivity	100.00	99.87	99.79	99.54	99.39	100.00	99.87	99.78	99.54	99.39

STEADY STATES ASSOCIATED WITH VARIOUS ANNUAL MONETARY GROWTH RATES RELATIVE TO THE BENCHMARK When $\theta_h = 1$

NOTES: The steady-states levels are reported in percentage points relative to the model that corresponds to the economy where the monetary growth rate is $g = \beta - 1$. ^aAverage U.S. inflation rate over the 1988–2007 period.

4.1 Steady-State Properties

We choose $g = (\beta - 1)$ as the benchmark monetary growth rate, which is the policy rule yielding the Pareto optimal allocation. Accordingly, Tables 3 and 4 report the level of each macroeconomic aggregate of interest and of average productivity relative to the levels corresponding to the Pareto optimal steady state. As shown in Tables 3 and 4, anticipated inflation has a significant impact on the long-run equilibrium of the economy. Steady-state output, consumption, investment, hours, and the number of establishments in the economy are all lower whenever the monetary growth rate exceeds $(\beta - 1)$. We begin by interpreting the results in each table.

Table 3 corresponds to model specifications where $\theta_h = 1$ and, hence, the entry cost is subject to the CIA constraint. The table includes four panels, each corresponding to an alternative configuration of the constraint. When the CIA constraint applies to the creation of new establishments, inflation discourages firm entry. Therefore, at high rates of inflation there are fewer incumbent establishments and the demand for labor is lower. As a result, the wage rate is lower allowing low productivity establishments to become active. Hence, the average productivity of incumbent establishments is lower at high rates of inflation. The bottom row of each panel of Table 3 reports the level of average productivity at various rates of money growth. Inspecting each panel reveals that the money growth rule affects productivity in the same way for each possible configuration of the CIA constraint as long as $\theta_h = 1$. When the annual rate of inflation is 10%, productivity, relative to the optimum, is 0.46% lower. Thus,

STEADY STATES ASSOCIATED WITH VARIOUS ANNUAL MONETARY GROWTH RATES RELATIVE TO THE BENCHMARK When $\theta_h = 0$

Annual inflation rate in %	$\begin{array}{c} 100 \times \\ (\beta^4 - 1) \end{array}$	0.00	2.43 ^a	10.00	15.00	$\begin{array}{c} 100 \times \\ (\beta^4-1) \end{array}$	0.00	2.43 ^a	10.00	15.00
	P	anel A:	$\theta_c = 1$ as	nd $\theta_k =$	1	F	anel B:	$\theta_c = 1$ as	nd $\theta_k =$	0
Output	100.00	98.88	98.17	96.09	94.82	100.00	99.27	98.83	97.52	96.72
Consumption	100.00	99.04	98.43	96.63	95.53	100.00	99.27	98.83	97.52	96.72
Investment	100.00	97.95	96.67	92.95	90.70	100.00	99.27	98.83	97.52	96.72
Hours	100.00	99.18	98.67	97.15	96.21	100.00	99.27	98.83	97.52	96.72
No. of establishments	100.00	98.88	98.17	96.09	94.82	100.00	99.27	98.83	97.52	96.72
Productivity	100.00	100.00	100.00	100.00	100.00	100.00	100.00	100.00	100.00	100.00
	F	anel C: ($\theta_c = 0$ as	nd $\theta_k =$	1	P	anel D:	$\theta_c = 0$ a	nd $\theta_k =$	0
Output	100.00	99.57	99.30	98.50	98.01	100.00	100.00	100.00	100.00	100.00
Consumption	100.00	99.73	99.56	99.06	98.74	100.00	100.00	100.00	100.00	100.00
Investment	100.00	98.64	97.78	95.28	93.76	100.00	100.00	100.00	100.00	100.00
Hours	100.00	99.88	99.80	99.58	99.45	100.00	100.00	100.00	100.00	100.00
No. of establishments	100.00	99.57	99.30	98.50	98.01	100.00	100.00	100.00	100.00	100.00
Productivity	100.00	100.00	100.00	100.00	100.00	100.00	100.00	100.00	100.00	100.00

NOTES: The steady-states levels are reported in percentage points relative to the model which corresponds to the economy where the monetary growth rate is $g = \beta - 1$. ^aAverage U.S. inflation rate over the 1988–2007 period.

increasing the monetary growth rate has a negative impact on average productivity which results directly from the fact that money holdings are a requirement for the creation of new establishments.

The results regarding the other macroeconomic aggregates are of course sensitive to the model specification. Examining Panel B of both Tables 3 and 4 illustrates the implications of anticipated inflation when consumption is subject to the CIA constraint. Agents facing high rates of inflation substitute away from consumption and toward leisure, which leads to lower output and therefore lower consumption and investment. Moreover, Panel B of Table 4 reveals that, even when the liquidity constraint only applies to the consumption good, still output and investment both fall proportionally, preserving the investment-output ratio, despite the fact that the investment good and the entry cost are not subject to the CIA constraint. This result follows from the fact that the purpose of increasing the capital stock is to provide consumption in the future, which is affected by the inflation tax in the same way as consumption today.

Another implication of our model economy is that the amount of time spent working is lower at higher rates of inflation, implying an upward sloping long-run Phillips curve. This finding is robust across model specifications.

Also, both Tables 3 and 4 show that as the monetary growth rate is increased, the number of incumbent establishments and equivalently the creation of new establishments lower substantially. There are two reasons why fewer establishments enter at high rates of inflation. First, since the purpose of creating new establishments is to

produce consumption in the future, which is subject to exactly the same inflation tax as consumption today, the creation of new establishments is discouraged at high rates of inflation. This happens even when the entry cost is not subject to the CIA constraint (Table 4). The second reason, which only intervenes when the entry cost is subject to the finance constraint (Table 3), has to do with the fact that the cost of creating new establishments increases as the monetary growth rate is raised. As the cost of creating new establishments is increased, the profits of incumbents must increase as well, which allows low-productivity establishments to stay in the industry. This adjustment in the size distribution of productive establishments implies that labor and capital are employed less efficiently, which lowers aggregate output and, consequently, the creation of new establishments.

Finally, Panel D in Table 4 simply illustrates that the CIA constraint is the only channel through which the economy is affected by changes in the rate of growth of money. In what follows, we investigate the welfare cost of inflation and we study more carefully the role played by firm heterogeneity.

4.2 Welfare Costs of Inflation

To obtain a measure of the welfare cost associated with inflation we proceed in the same way as in Cooley and Hansen (1989). In particular, we compute the increase in steady-state consumption which an individual would require at a given rate of money growth, g, to be as well off as under the optimal monetary policy rule, which achieves the Pareto optimal allocation. Thus, to compute the welfare cost associated with variations in the monetary growth rate, we solve for $W \equiv \Delta C/C$ in the equation

$$\bar{U} = \ln \left[(1 + \mathcal{W}) C \right] + A \ln (1 - N),$$
(22)

where \bar{U} is the level of utility attained in steady state under the optimal monetary policy rule, $g = \beta - 1$, and *C* and *N* are the steady-state consumption and hours associated with the monetary growth rate g.¹³

Table 5 shows our findings. The left-hand side panel corresponds to the specifications where the CIA constraint applies to the entry cost and the right-hand side panel considers the other cases. When the CIA constraint does not apply to the sunk cost the welfare costs of inflation we obtain are of the same order of magnitude as the ones obtained by Cooley and Hansen (1989). In particular, when only consumption is subject to the CIA constraint—the specification that corresponds more closely to the Cooley and Hansen model—the welfare cost of a 10% rate of inflation is 0.46% of steady-state consumption. This is roughly the same cost which is reported in Cooley and Hansen (1989).

However, when the CIA constraint applies to the entry cost, the welfare cost of inflation is almost doubled. For example, the welfare cost of a 10% rate of inflation

¹³ The solution for the welfare cost of inflation is derived in close form in Appendix B.4 (available from the authors' website).

		θ_h	= 1		$\theta_h = 0$			
	$\theta_c = 1$	$\theta_c = 1$	$\theta_c = 0$	$\theta_c = 0$	$\theta_c = 1$	$\theta_c = 1$	$\theta_c = 0$	$\theta_c = 0$
100 × g	$\theta_k = 1$	$\boldsymbol{\theta}_k = \boldsymbol{0}$	$\theta_k = 1$	$\boldsymbol{\theta}_k = \boldsymbol{0}$	$\theta_k = 1$	$\boldsymbol{\theta}_k = \boldsymbol{0}$	$\theta_k = 1$	$\theta_k = 0$
$100 \times (\beta^4 - 1)$	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000
0.00	0.393	0.239	0.274	0.113	0.286	0.125	0.168	0.000
2.43ª	0.651	0.389	0.451	0.182	0.474	0.205	0.276	0.000
10.00	1.451	0.857	0.986	0.391	1.057	0.456	0.601	0.000
15.00	1.975	1.165	1.326	0.524	1.439	0.624	0.807	0.000
20.00	2.495	1.470	1.658	0.652	1.818	0.791	1.007	0.000
40.00	4.527	2.669	2.901	1.129	3.300	1.462	1.752	0.000

Welfare Costs Associated with V	VARIOUS ANNUAL	GROWTH RATES	OF MONEY
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Notes: The measure of the welfare cost of inflation is $\Delta C/C \times 100$ where ΔC is the consumption compensation needed for the representative agent to achieve the same steady state utility associated with the optimal monetary policy rule.

when consumption and the entry cost are subject to the cash constraint is 0.86% of steady-state consumption. A substantial part of the welfare losses at high rates of inflation are explained by the lower efficiency in the allocation of resources across incumbent establishments and not just by less accumulation of factors of production. Contrasting the second row of the left-hand side panel and the second row of the right-hand side panel shows that when the CIA constraint applies to the creation of

new establishments the welfare cost of inflation nearly doubles.

If all three goods are subject to the CIA constraint, the welfare cost of 10% inflation is 1.45% of steady-state consumption. Thus, the cost of inflation resulting from lower investment and time spent working can be substantially amplified by the fall in the wage rate implied by the distortion to the establishments' entry and exit dynamics. Finally, if only the entry cost is subject to the CIA constraint, the welfare cost of 10% inflation is 0.39% of steady-state consumption.

4.3 The Role of Returns to Scale

Atkeson, Khan, and Ohanian (1996) forcefully show that the choice of the returns to scale in models with industry dynamics is an important determinant of the size of the effect of policy distortions on average productivity and welfare.¹⁴ Therefore, in this section we consider how sensitive our estimates of the welfare costs of inflation are to changes in the returns to scale. Returns to scale matter because of the following intuition: as anticipated inflation increases, low-productivity establishments enter the industry because factor prices decrease; factor prices will decrease by more, the more concave the profit function is, that is, the lower the returns to scale.

^{14.} Moreover, it should be noted that Atkeson, Khan, and Ohanian (1996) present evidence against the hypothesis that plant production or profit functions are nearly linear. This offers support to the view that policy distortions have sizable effects.

$\alpha + \nu$	$100 imes rac{\Delta ar{s}}{ar{s}}$	$\frac{\theta_h = 0}{100 \times \mathcal{W}}$	$\frac{\theta_h = 1}{100 \times \mathcal{W}}$	Share of welfare cost explained by fall in \bar{s}
0.75	-0.73	0.43	1.05	0.59
0.80	-0.60	0.44	0.96	0.54
0.85	-0.46	0.46	0.86	0.47
0.90	-0.32	0.47	0.74	0.37
0.95	-0.16	0.47	0.62	0.23
0.99	-0.03	0.48	0.51	0.06

LADLE U

WELFARE COSTS CORRESPONDING TO DIFFERENT DEGREES OF DIMINISHING RETURNS TO SCALE

Notes: The measure of the welfare cost of inflation is W, the percentage increase in consumption required to for the representative agent to achieve the same steady-state utility associated with the Pareto optimum allocation, when the annual inflation rate is 10%. For each model specification consumption is subject to the CIA constraint ($\theta_c = 1$) but investment is not ($\theta_k = 0$).

As expected, we show that as $\alpha + \nu$ approaches one, productivity is no longer affected by changes in the monetary growth rate and the contribution of factors reallocation to the welfare cost of inflation disappears. However, this contribution increases at a high rate, as the intensity of diminishing returns increases.

Table 6 shows the average productivity associated with different degrees of diminishing returns to scale and the corresponding welfare cost of inflation. For each model specification consumption is subject to the CIA constraint but investment is not—Cooley and Hansen's (1989) specification. This allows us to understand the role of productivity in explaining the welfare cost of inflation for different degrees of diminishing returns. Once again, we consider the welfare cost of 10% inflation.

Naturally, when the returns to scale are nearly constant, $\alpha + \nu = 0.99$, the productivity is almost not affected as the monetary growth rate is increased. Indeed, average productivity is only 0.03% lower at 10% inflation, compared to the level under the optimal policy. Hence, the welfare costs of inflation are roughly the same, irrespective of whether the CIA constraint applies to the entry cost or not. The last column of Table 6 shows how distortions to the size distribution of productive establishments contribute to the welfare costs of inflation.¹⁵ As expected, when the returns to scale are nearly constant this contribution is very small. However, the contribution increases quickly, as the intensity of diminishing returns increases. Indeed, for the range of $\alpha + \nu$ between 0.75 and 0.90 the contribution of distortions to the size distribution of incumbents is sizable, taking values between 37% and 59% of the total welfare cost of inflation.

As the intensity of diminishing returns increases, the share of welfare cost explained by a fall in average productivity increases (see the last column in Table 6). This happens for two reasons. First, as returns diminish faster, the distortions to the size distribution of establishments, resulting from the inflation tax, are more important and lead to significant falls in average productivity. Thus, when the CIA constraint

^{15.} We quantify this by computing the percentage increase in the welfare cost of inflation when the CIA constraint applies to the entry cost.

applies to the entry cost ($\theta_h = 1$) the welfare cost of inflation is high. However, an additional reason why the contribution of falls in average productivity to the welfare cost of inflation increases at lower values of $\alpha + \nu$ is that when $\theta_h = 0$, the welfare cost of inflation increases as the intensity of diminishing returns to scale decreases. This is because, when $\theta_h = 0$, the welfare cost is explained by the fall in the accumulation of factors. Thus, when $\alpha + \nu$ is low, the falls in output and welfare associated with the inflation tax are less important.

Overall, for values of $\alpha + \nu$ between 0.75 and 0.90, the contribution of distortions to the size distribution of productive establishments is substantial. Indeed, when the entry cost is subject to the CIA, the welfare cost of 10% anticipated inflation varies between 0.74% and 1.05% of steady-state consumption.

4.4 Increasing Returns to Scale

The empirical evidence for decreasing returns to scale is mixed. While Atkeson and Kehoe (2005) consider a value equal to 0.85, Basu and Fernald (1997) show that empirical estimates depend on the level of aggregation. They often rise at higher levels of aggregation. Some authors even obtain increasing returns such as Laitner and Stolyarov (2004), whose estimates set the output elasticity at about 1.1 by use of growth accounting techniques. In this section, we introduce a modified version of the model where we allow for increasing returns to scale and monopolistic competition.¹⁶

The result we want to emphasize is that whatever the nature of returns to scale is, what matters is the concavity of the profit function. When the profit function is concave, factor prices decrease as the rate of anticipated inflation increases causing low-productivity firms to enter the industry. Thus, in a standard setting with monopolistic competition our earlier analysis still holds with increasing returns to scale as long as the profit function remains concave. If complementary between varieties is high enough, the results of the previous sections go through because the profit function remains concave.

Suppose aggregate output results from production by a single representative firm in the final-good sector. This firm takes prices as given and uses series of intermediate goods in the production process. Intermediate goods are the only factors this firm uses. The production function is the following:

$$Y_{t} = \left[H_{t}^{\rho-1} \int_{j} y_{j,t}^{\rho} dj\right]^{1/\rho},$$
(23)

^{16.} However, notice that in the benchmark model the economy exhibits constant returns to scale at the aggregate level despite the assumption of decreasing returns to the variable factors at the firm level. At the firm level the production function displays decreasing returns in the variable factors, i.e., $(\alpha + \nu) < 1$, but the fixed operating cost η brings about increasing returns to scale. The upshot is that, in equilibrium, the aggregate production function exhibits constant returns to scale. We thank an anonymous referee for pointing this out to us. The aggregate production function function function function is derived in Appendix B.6 (available from the authors' website).

where *j* refers to a particular variety of input used in quantities $y_{j,t}$, H_t is the mass of intermediate goods and $\rho \in (0, 1)$ is a parameter that determines the elasticity of substitution between inputs, which is equal to $1/(1 - \rho)$. The term $H_t^{\rho-1}$ is introduced to remove any love for variety in the production process.¹⁷ The absence of love for variety undermines the welfare cost of inflation and takes us to a framework closer to the one presented in the previous sections. In a context with love for variety, the cost would be larger.

In the intermediate goods sector, firms behave closely to the firms from the preceding sections with the exception that there is now monopolistic competition \hat{a} la Dixit and Stiglitz (1977) in this sector: they can choose the price $p_{j,t}$ at which they sell their goods to the final-good firm.

The assumptions regarding heterogeneity in productivity and free entry are kept for the intermediate-goods sector. The production function for a firm selling input *j* with productivity s_j is given by $\tilde{y}_{j,t} = s_j n_{j,t}^{\alpha} k_{j,t}^{\nu}$ with $(\alpha + \nu)\rho < 1$.

Average productivity in the stationary equilibrium is now defined as

$$\bar{s} = \left[\int_{s^*}^{\infty} s^{\tilde{\sigma}\rho} \frac{dF(s)}{1 - F(s^*)} \right]^{\frac{1}{\tilde{\sigma}\rho}},\tag{24}$$

with $\tilde{\sigma} = 1/[1 - \rho(\alpha + \nu)].$

Finally, aggregate output can be used for consumption, investment, and the payment of both the entry cost κ and the fixed operating cost η paid by the intermediate-good establishments.

It can be shown that the demand for input *j* is described by the following equation:

$$y_{j,t} = \frac{Y}{H} p_{j,t}^{-1/(1-\rho)},$$
(25)

which implies that the profit function for the establishment producing input j can be written as

$$z_{j,t} = y_{\bar{s}_t,t}^{-\rho} y_{j,t}^{\rho} - w_t n_{j,t} - r_t k_{j,t} - \eta,$$
(26)

where $y_{\bar{s}_t,t}$ is the level of output for a firm producing an intermediate good with average productivity \bar{s}_t . Notice that equation (26) is identical to the flow profits in equation (5), except for the presence of term $y_{\bar{s}_t,t}$.

Two things have to be pointed out in this equation. First, as ρ moves from one to zero—hence, as goods become more complementary—the profit function becomes more concave. In particular, to get the same concavity as in the model with perfect competition, we need $\rho(\alpha + \nu) = \sigma$, where σ refers to the parameter introduced in Section 1.2. Second, because the marginal productivity of inputs in the final-good sector is an increasing function of $y_{t,\bar{s}}$, the level of output of a firm with the average

^{17.} As an illustration, suppose that, for all $j, y_{j,t} = \tilde{y}$, then, because of this term, $Y_t = H_t \tilde{y}$. See Benassy (1996) and Blanchard and Giavazzi (2003).

			3.8	Elasticity of subs	stitution: $1/(1 - \rho)$)	6.0	
$\alpha + \nu$	$100 imes rac{\Delta ar{s}}{ar{s}}$	$\frac{\theta_h = 1}{100 \times \mathcal{W}}$	$\frac{\theta_h = 0}{100 \times \mathcal{W}}$	Share due to \bar{s}	$100 imes rac{\Delta ar{s}}{ar{s}}$	$\frac{\theta_h = 1}{100 \times \mathcal{W}}$	$\frac{\theta_h = 0}{100 \times \mathcal{W}}$	Share due to \bar{s}
1.01	-0.96	1.71	0.72	0.57	-0.57	1.19	0.63	0.47
1.05	-0.87	1.63	0.73	0.55	-0.46	1.09	0.64	0.41
1.10	-0.75	1.52	0.75	0.51	-0.32	0.96	0.65	0.32
1.15	-0.62	1.40	0.76	0.46	-0.16	0.82	0.66	0.20
1.19	-0.51	1.29	0.76	0.41	-0.03	0.69	0.66	0.04

WELFARE COSTS IN THE IRS MODEL WITH MONOPOLISTIC COMPETITION

Notes: The measure of the welfare cost of inflation is W, the percentage increase in consumption required to for the representative agent to achieve the same steady-state utility associated with the Pareto optimum allocation, when the annual inflation rate is 10%. For each model specification consumption is subject to the CIA constraint ($\theta_c = 1$) but investment is not ($\theta_k = 0$).

productivity influences more individual profits as ρ moves from one to zero. This externality is standard in models with monopolistic competition and does not depend on the presence of love for variety.

Table 7 gives the same sort of information as Table 6 for the modified version of the model with increasing returns and monopolistic competition. In this table, we consider two values for the elasticity of substitution: 3.8 taken from Bernard et al. (2003) and 6 from Rotemberg and Woodford (1992). The first value was calibrated to fit U.S. plant and macro trade data, while the second had been considered to deliver a 20% markup of price over marginal cost. We also consider several values for the returns to scale ranging from 1.01 to 1.19. This range contains the 1.1 value estimated by Laitner and Stolyarov (2004).

The table shows that, as the profit function becomes more concave—i.e., as either ρ or $\alpha + \nu$ decrease—the welfare cost of inflation becomes larger. Moreover, the share of the cost due to the decrease in average productivity also rises.¹⁸ These results are in line with those displayed in Table 6. Moreover, from a quantitative perspective, the effect of inflation is larger in the modified version of the model because of the aggregate externality. As an illustration, consider the values $1/(1 - \rho) = 6$ and $\alpha + \nu = 1.01$, which imply $\rho(\alpha + \nu) \approx 0.85$. For those values, which deliver the same concavity of the profit function as before, the share of the cost due to the fall in average productivity is the same (47%), but the welfare cost of inflation is larger: the decrease in aggregate consumption is 1.19%, while it is 0.86% in the model with perfect competition. Notice also that the importance of the mechanism we illustrate in this paper is bigger for values which are in line with Bernard et al. (2003) and Laitner and Stolyarov (2004). In this case, the welfare cost of inflation amounts to 1.52%, with 51% explained by the decrease in average productivity.

^{18.} In this table, the values concerning the decrease in productivity cannot be compared to the values in Table 6 because the definition of average productivity is different.

Heterogeneity $\left(\frac{1}{\epsilon - \sigma}\right)$	$100 imes rac{\Delta ar{s}}{ar{s}}$	$\frac{\theta_h = 0}{100 \times \mathcal{W}}$	$\frac{\theta_h = 1}{100 \times \mathcal{W}}$	Share of welfare cost explained by fall in \bar{s}
0.01	-0.03	0.33	0.35	0.07
0.50	-0.39	0.43	0.77	0.43
1.00	-0.44	0.45	0.83	0.46
1.67	-0.46	0.46	0.86	0.47
2.00	-0.47	0.46	0.87	0.47
5.00	-0.49	0.46	0.89	0.48

TABLE	8
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WELFARE COSTS CORRESPONDING TO DIFFERENT DEGREES OF ESTABLISHMENT HETEROGENEITY

Notes: The measure of the welfare cost of inflation is W, the percentage increase in consumption required to for the representative agent to achieve the same steady-state utility associated with the Pareto optimum allocation, when the annual inflation rate is 10%. For each model specification consumption is subject to the CIA constraint ($\theta_c = 1$) but investment is not ($\theta_k = 0$).

4.5 The Role of Firm Heterogeneity

When the entry cost is subject to the cash constraint the level of heterogeneity turns into an important determinant of the way changes in the monetary growth rate affect the economy: the larger the heterogeneity, the larger is the fall in productivity. Here, we investigate what happens to the estimate of the welfare cost of inflation as we change the level of firm heterogeneity.

Table 8 shows different welfare cost estimates as we vary the amount of establishment heterogeneity, for two different models specifications—when $\theta_h = 0$ and when $\theta_h = 1$.¹⁹ As the dispersion of establishments' productivities increases, the fall in productivity, associated with an increase in the rate of inflation, varies from 0.03% to 0.49%. In particular, when there is almost no heterogeneity—i.e., $(\epsilon - \sigma)^{-1} = 0.01$ —productivity is virtually not affected by the inflation tax. Moreover, as the level of heterogeneity falls to zero, productivity is not affected by changes in the monetary growth rate and, accordingly, the welfare cost of anticipated inflation is the same no matter whether the entry cost is subject to the finance constraint or not. This illustrates clearly that the mechanism proposed in this paper intervenes through the productivity channel.

Furthermore, we notice that as the level of heterogeneity increases toward empirically relevant values, the sensitivity of productivity to the inflation tax increases quickly. For instance, if the standard deviation of log output is 0.50 (which is about one third of our benchmark calibration), at a 10% monetary growth rate, productivity is lowered by 0.39% and the welfare cost of inflation increases substantially. Therefore, we conclude that our findings are robust to changes in the variability of establishment productivity draws over the empirically relevant range.

^{19.} Once again, for each model specification consumption is subject to the CIA constraint but investment is not (Cooley and Hansen's 1989 specification).

4.6 Transition Dynamics

To evaluate policy reforms it is interesting to consider the transition path, as the economy moves from a given steady state associated with a monetary growth rate to the new steady state associated with optimal monetary policy. In this section we examine the welfare cost of inflation taking into account the adjustment path after the implementation of the optimal policy. Two results stand out. First, as expected the welfare cost of inflation is smaller when we consider the transition dynamics. Second, adjustments in average productivity play a more prominent role when we consider the transition path after the policy reform.

We apply perturbation methods to study the transition dynamics after the implementation of the optimal policy. Specifically, we log-linearize the model around the Pareto optimal steady state and consider the transition dynamics starting from the suboptimal steady state. In Appendix B.2 (available from the authors' website), the system of equations characterizing the equilibrium is summarized. We can reduce the system in Appendix B.2 to a system of two equations in two variables, H_t and s_t^* (see Appendix B.3, available from the authors' website, for a detailed description). Using \tilde{x} to denote log-deviations from steady state of the variable *X*, log-linearization around the steady state yields

$$\begin{bmatrix} \Sigma_{11} & \Sigma_{12} \\ \Sigma_{21} & \Sigma_{22} \end{bmatrix} \begin{bmatrix} \tilde{h}_{t+1} \\ \tilde{s}_{t+1}^{\star} \end{bmatrix} = \begin{bmatrix} \Gamma_{11} & \Gamma_{12} \\ \Gamma_{21} & \Gamma_{22} \end{bmatrix} \begin{bmatrix} \tilde{h}_t \\ \tilde{s}_t^{\star} \end{bmatrix},$$
(27)

where the number of incumbent firms in log-deviation from steady state, \tilde{h}_t , is the state variable and \tilde{s}_t^* , the productivity threshold in log-deviation from steady state, is the control variable.²⁰

20. The Σ_{ij} and Γ_{ij} parameters are given by

$$\begin{split} \Sigma_{11} &= \bar{K} + \kappa \bar{H}, \qquad \Sigma_{12} = \bar{K} \left(\frac{\lambda - \delta}{\bar{r}} \right) \varepsilon, \\ \Sigma_{21} &= \bar{N} / (1 - \bar{N}), \quad \Sigma_{22} = \left[\frac{(1 + \varepsilon \nu)\bar{r} + (\lambda - \delta)\nu\varepsilon}{\alpha \bar{r} (1 - \bar{N})} + \left(\frac{\bar{N}}{1 - \bar{N}} \right) \varepsilon + \beta (\lambda + \bar{r} - \delta) \varepsilon \right] \end{split}$$

and

$$\begin{split} &\Gamma_{11} = \bar{Y} + \bar{C} \left(\frac{\bar{N}}{1 - \bar{N}} \right) + (1 - \delta) \,\bar{K} + (1 - \lambda) \,\bar{H}\kappa, \\ &\Gamma_{12} = \bar{C} \left(\frac{\bar{N}}{\bar{N} - 1} \right) \left[\varepsilon + \frac{(1 + \varepsilon \upsilon) \,\bar{r} + (\lambda - \delta) \,\upsilon \varepsilon}{\alpha \bar{r} \bar{N}} \right] - \left[\bar{Y} - (1 - \delta) \,\bar{K} \left(\frac{\lambda - \delta}{\bar{r}} \right) \right] \varepsilon \\ &\Gamma_{21} = \bar{N} / \left(1 - \bar{N} \right), \\ &\Gamma_{22} = \left[\frac{(1 + \varepsilon \upsilon) \,\bar{r} + (\lambda - \delta) \,\upsilon \varepsilon}{\alpha \bar{r} \left(1 - \bar{N} \right)} + \left(\frac{\bar{N}}{1 - \bar{N}} \right) \varepsilon \right]. \end{split}$$

$100 \times g$		θ_h	= 1		$\theta_h = 0$			
	$\begin{array}{c} \theta_c = 1 \\ \theta_k = 1 \end{array}$	$\begin{array}{l} \theta_c = 1 \\ \theta_k = 0 \end{array}$	$\begin{array}{l} \theta_c = 0 \\ \theta_k = 1 \end{array}$	$\begin{array}{c} \theta_c = 0 \\ \theta_k = 0 \end{array}$	$\begin{array}{c} \theta_c = 1 \\ \theta_k = 1 \end{array}$	$\begin{array}{l} \theta_c = 1 \\ \theta_k = 0 \end{array}$	$\begin{array}{l} \theta_c = 0 \\ \theta_k = 1 \end{array}$	$\begin{array}{c} \theta_c = 0 \\ \theta_k = 0 \end{array}$
2.43 ^a 10.00 20.00 40.00	0.278 0.638 1.133 2.156	0.116 0.272 0.498 0.993	0.261 0.574 0.975 1.730	0.103 0.222 0.374 0.657	0.177 0.410 0.737 1.426	0.012 0.042 0.105 0.282	0.161 0.354 0.598 1.055	0.000 0.000 0.000 0.000

WELFARE COSTS	TAKING	INTO	ACCOUNT	THE	TRANSITION	PATH

Notes: The measure of the welfare cost of inflation is $W' \times 100$. ^aAverage U.S. inflation rate over the 1988–2007 period.

The alternative welfare measure, which takes into account the transitional dynamics, is obtained by solving for the sequence of consumption and time spent working after the implementation of the optimal policy, $\{C_t^o\}_{t=t0}^T$ and $\{N_t^o\}_{t=t0}^T$ (where t_0 is

after the implementation of the optimal policy, $\{C_t^o\}_{t=t0}^T$ and $\{N_t^o\}_{t=t0}^T$ (where t_0 is the period in which the optimal policy is first implemented and T is a much later period—we consider T = 10,000) and comparing the utility under the optimal policy with the utility in the suboptimal steady state associated with the monetary growth rate g. Specifically, the welfare cost is calculated by equating the following expression to zero and solving for W':

$$\sum_{s=0}^{T} \beta^{s} \{ \left[\ln C(1+\mathcal{W}') + A \ln(1-N) \right] - U^{o}_{t_{0}+s} \},$$
(28)

where $U_{t_0+s}^o \equiv \ln C_{t_0+s}^o + A \ln(1 - N_{t_0+s}^o)$ is the flow utility in period $t_0 + s$ under the optimal monetary policy and *C* and *N* are consumption and time spent working in steady state, in an economy where the monetary growth rate is *g*.

Table 9 considers the welfare gain of reducing the monetary growth rate and adopting the optimal monetary policy. The left-hand side panel corresponds to the specifications where the CIA constraint applies to the entry cost and the right-hand side panel considers the other cases. Two results stand out. First, as expected the welfare cost obtained taking into account the transition path is smaller than the alternative measure, which only considers the steady states.²¹ After the implementation of the new policy the number of establishments and the capital stock increases only gradually. Therefore, it takes time for consumption to reach the new steady-state level and leisure must be sacrificed along the transition path. As a consequence, the flow utility only slowly attains the new steady state. However, the transition dynamics do not overturn the welfare results overwhelmingly. For instance, when the CIA constraint applies to consumption and to the entry cost, the welfare cost of 10% inflation is 0.272% of steady-state consumption.

The second important result has to do with the comparison between the cases when $\theta_h = 0$ and when $\theta_h = 1$. Comparing the left-hand-side panel with the right-hand-

^{21.} Comparing Table 9 and Table 5.



FIG. 4. Transition Dynamics after Implementation of the Optimal Policy: Solid Line Corresponds to the Case Where $\theta_h = 0$; the Dashed Line to the Case Where $\theta_h = 1$.

side panel of Table 9, we see that when the CIA constraint applies to the entry cost the welfare cost of inflation is amplified. For instance, for the specification where the CIA constraint applies to consumption but not to investment—the specification considered by Cooley and Hanson (1989)—the welfare cost of 10% inflation is 0.272% of steady-state consumption when $\theta_h = 1$ and only 0.042% of steady-state consumption when $\theta_h = 0$. Thus, considering the transition dynamics, the welfare cost of 10% inflation is almost an order of magnitude higher when the size distribution of productive establishments is affected by the monetary growth rate.

To understand better these findings we show the transition path of the relevant variables. Figure 4 shows the time path of H_t , s_t^* , K_t , C_t , N_t , w_t , r_t , and U_t after the implementation of the optimal policy for the cases $\theta_h = 1$ and $\theta_h = 0$, respectively. We consider first the case where the entry cost is subject to the CIA constraint-i.e., the case $\theta_h = 1$ (dashed line). After the implementation of the optimal monetary policy productivity jumps upward immediately and begins converging to the new (higher) steady-state level. The number of incumbent establishments and the capital stock increases gradually. Consumption also jumps upward and starts converging toward the higher steady state. However, as consumption is below the new steady state on the transition path, time spent working increases substantially and in fact overshoots vis-à-vis the new steady state. This is because of intertemporal substitution: as the marginal utility of consumption is high with respect to the new steady-state agents enjoy relatively less leisure on the transition path. Since consumption adjusts only slowly to the new steady state and agents enjoy less leisure after the implementation of the new policy, the flow utility level decreases first and starts converging gradually to the new higher level. In fact, the flow utility level surpasses the initial level 9 years (36 quarters) after the implementation of the new policy.

The transition path of productivity is very different when the entry cost is not subject to the CIA constraint—i.e., the case $\theta_h = 0$ (solid line). In this case, we know from Proposition 1 that the steady-state productivity level is not affected. However, in the short-run the threshold productivity level actually falls after the implementation of the optimal policy. This happens because in the short run the increase in labor supply following the implementation of the new policy lowers the wage rate. At the lower wage rate, firms that before were not sufficiently productive now decide to stay active. Therefore, the productivity distribution is shifted to the left and the productivity threshold falls. Along the transition path the productivity threshold converges gradually to the initial level. The upshot of this adjustment path is that the welfare cost of not implementing the optimal policy is lower when the entry cost is not subject to the CIA constraint.

5. CONCLUSION

In this paper, we set out to investigate whether it is important to model heterogeneity across productive establishments when quantifying the welfare cost of inflation. For this purpose, we study a model characterized with a CIA constraint on consumption and investment goods, and in addition we assume that the CIA constraint also applies to the creation of new establishments. This assumption is motivated by substantial evidence that finance constraints are often binding constraints facing aspiring entrepreneurs.

Two results come out of our analysis. First, anticipated inflation lowers aggregate productivity. This happens because an increase in the long-run rate of money growth increases the cost of creating new establishments and distorts firm entry dynamics. As a consequence, the number of incumbent establishments and the demand for labor fall, resulting in lower wages. With lower wages, less productive establishments choose to produce, lowering average productivity. This opens a channel through which inflation may affect welfare which received little attention in the literature. Second, the mechanism identified in the current paper is likely to be quantitatively important. In particular, our results suggest that the adjustment in the productivity distribution of incumbent establishments is responsible for about half of the welfare cost of inflation.

As was mentioned earlier, Baily, Hulten, and Campbell (1992) document that about half of overall productivity growth in U.S. manufacturing in the 1980s can be attributed to factor reallocation from low-productivity to high-productivity establishments. It is tempting to imagine that the sustained disinflation which occurred over the same period may have contributed to the reallocation of factors and improvements in efficiency.

APPENDIX

A.1 Locally Vertical WW Locus

The purpose of this section is to show that the WW locus is locally vertical. Hence, equilibrium wage rate w and s^* are independent. To do this, we apply the implicit function theorem to the relationship (20) with the purpose of finding dw/ds^* . First, notice that the relationship (20) can be rewritten as

$$\kappa \left[1 + \theta_h \left(\frac{1+g}{\beta} - 1 \right) \right] \frac{1 - \beta(1-\lambda)}{\beta} + [1 - F(s^*)]\eta - \frac{\Omega \int_{s^*}^{\infty} s^{\sigma} dF(s)}{w^{\alpha\sigma} r^{\nu\sigma}} = 0,$$
(A1)

which can simply be written as $\Phi(s^*, w) = 0$. Moreover, by the implicit function theorem $dw/ds^* = -\frac{\partial \Phi(s^*, w)}{\partial s^*} / \frac{\partial \Phi(s^*, w)}{\partial w}$. Since

$$\frac{\partial \Phi\left(s^{\star},w\right)}{\partial w} = \frac{\alpha \sigma \Omega}{w^{1+\alpha\sigma} r^{\nu\sigma}} \int_{s^{\star}}^{\infty} s^{\sigma} dF(s) > 0,$$

a sufficient and necessary condition for $dw/ds^* = 0$ is simply $\partial \Phi(s^*, w)/\partial s^* = 0$. In turn

$$\frac{\partial \Phi\left(s^{\star},w\right)}{\partial s^{\star}} = f\left(s^{\star}\right) \left(\frac{\Omega s^{\star\sigma}}{w^{\alpha\sigma} r^{\nu\sigma}} - \eta\right) = 0,$$

because equation (21) implies that in equilibrium $\Omega s^{*\sigma} w^{-\alpha\sigma} r^{-\nu\sigma} = \eta$. Therefore, $dw/ds^* = 0$ and the WW locus is locally vertical.

A.2 Existence and Uniqueness of Equilibrium

This section contains a proof that equations (20) and (21) always define a unique equilibrium.²² The condition (20) implies an expression for average profits, given by

$$\bar{z} = \kappa \left[1 + \theta_h \left(\frac{1+g}{\beta} - 1 \right) \right] \frac{\frac{1}{\beta} - 1 + \lambda}{1 - F(s^\star)}.$$
(A2)

In turn, combining the equations (17) and (21) implies that average profits must satisfy the equilibrium condition given by

$$\bar{z} = \eta \left[\left(\frac{\bar{s}}{s^{\star}} \right)^{\sigma} - 1 \right].$$
(A3)

Consequently, a sufficient condition for ensuring the existence and uniqueness of s^* is that

$$j(\hat{s}) = [1 - F(\hat{s})] \left[\left(\frac{\bar{s}(\hat{s})}{\hat{s}} \right)^{\sigma} - 1 \right],$$

be monotonically decreasing from infinity to zero on $(0, \infty)$, where

$$\bar{s}\left(\hat{s}\right)^{\sigma} = \frac{1}{1 - F\left(\hat{s}\right)} \int_{\hat{s}}^{\infty} s^{\sigma} dF\left(s\right).$$

Define

$$\iota(\hat{s}) = \left(\frac{\bar{s}(\hat{s})}{\hat{s}}\right)^{\sigma} - 1.$$

By applying the Chain and Leibniz rules, the derivative of $\iota(\hat{s})$ with respect to \hat{s} is found to be

$$\iota'(\hat{s}) = \frac{f(\hat{s})}{1 - F(\hat{s})} \left[\left(\frac{\bar{s}(\hat{s})}{\hat{s}} \right)^{\sigma} - 1 \right] - \frac{\sigma}{\hat{s}} \left(\frac{\bar{s}(\hat{s})}{\hat{s}} \right)^{\sigma}$$
(A4)

$$=\frac{\iota\left(\hat{s}\right)f\left(\hat{s}\right)}{1-F\left(\hat{s}\right)}-\frac{\sigma\iota\left(\hat{s}\right)+\sigma}{\hat{s}}.$$
(A5)

22. A similar argument for proving existence and uniqueness of equilibrium in this class of heterogeneous firm models can be found in Melitz (2003).

Thus, the derivative and elasticity of $j(\hat{s})$ are given by

$$j'(\hat{s}) = -\frac{\sigma}{\hat{s}} \left(\iota(\hat{s}) + 1 \right) \left[1 - F(\hat{s}) \right] < 0,$$
(A6)

$$\frac{j'(\hat{s})\,\hat{s}}{j(\hat{s})} = -\sigma\left(1 + \frac{1}{\iota(\hat{s})}\right) < -\sigma. \tag{A7}$$

Since $j(\hat{s})$ is nonnegative and its elasticity with respect to \hat{s} is strictly negative, $j(\hat{s})$ must be decreasing to zero as \hat{s} goes to infinity. Moreover, $\lim_{\hat{s}\to 0} j(\hat{s}) = \infty$ since $\lim_{\hat{s}\to 0} \iota(\hat{s}) = \infty$. Hence, $j(\hat{s})$ is monotonically decreasing from infinity to zero on $(0, \infty)$ as needed to be proved.

A.3 Proof of Proposition 1

Following is a proof of Proposition 1. Thus, we analyze in more details the effect of anticipated inflation when one of the θ_i 's takes value one.

Case where $\theta_c = 1$, $\theta_k = 0$, and $\theta_h = 0$. We consider first the case where $\theta_c = 1$, $\theta_k = 0$, and $\theta_h = 0$. Notice that in this context inflation does not affect the rental cost of capital in (19), nor the productivity threshold and the wage rate in (20) and (21). From (4), (6), (7), and (8), this implies that average output, employment, capital use, and profits are also not affected by inflation.

To determine the effect of inflation on the other aggregates, notice that in the stationary equilibrium $X = \delta K = \delta \bar{k} H$, $\kappa E = \kappa \lambda [1 - F(s^*)]^{-1} H$ and $Y = \bar{y} H$. Replace those equations and (18) in (14) to get:

$$\frac{Lw}{A\left[1+\theta_c\left(\frac{1+g}{\beta}-1\right)\right]}+\delta\bar{k}H+\kappa\frac{\lambda}{1-F(s^{\star})}H=\bar{y}H.$$
(A8)

Given the labor-market clearing condition, we can write $L = 1 - N = 1 - \bar{n}H$. Replacing this relationship in the above equation and rearranging terms lead to:

$$H = \frac{w}{A\left[1 + \theta_c \left(\frac{1+g}{\beta} - 1\right)\right]} \times \left(\bar{y} - \delta \bar{k} - \kappa \frac{\lambda}{1 - F(s^*)} + \frac{w\bar{n}}{A\left[1 + \theta_c \left(\frac{1+g}{\beta} - 1\right)\right]}\right)^{-1}.$$
(A9)

Equation (A9) shows that when $\theta_c = 1$, an increase in the anticipated rate of inflation g decreases the mass of incumbent firms H. Given that average employment, capital,

and output are not affected, this implies that an increase in the anticipated rate of inflation g also decreases the aggregate level of capital, employment, and output.

Case where $\theta_c = 0$, $\theta_k = 1$, and $\theta_h = 0$. When $\theta_k = 1$, equation (19) shows that an increase in *g* increases the rental cost of capital *r*. To determine the effect of inflation on the productivity threshold and the wage rate in this context we use condition (A3). Replacing this relationship in the free-entry condition (20), we then have

$$\kappa \left[1 + \theta_h \left(\frac{1+g}{\beta} - 1 \right) \right] = \left[1 - F(s^\star) \right] \frac{\beta}{1 - \beta(1-\lambda)} \eta \left[\left(\frac{\bar{s}}{s^\star} \right)^\sigma - 1 \right].$$
(A10)

Hence, the productivity threshold does not depend on the rental cost of capital. Following an increase in g, the negative effect of the increase in r on profits cancels out with the positive effect of a decrease in wages. This latter can be seen from equations (19), (21), and (A10).

Regarding the effect of inflation on average output per establishment, remark that, from equations (4), (6), and (7), average output can be written as

$$\bar{y} = \bar{s}^{\sigma} \left(\frac{\alpha}{w}\right)^{\alpha\sigma} \left(\frac{\nu}{r}\right)^{\nu\sigma}.$$
(A11)

By replacing (21) in the above equation, one gets

$$\bar{y} = \frac{\eta}{\Omega} \left(\frac{\bar{s}}{s^{\star}}\right)^{\sigma} \alpha^{\alpha\sigma} v^{\nu\sigma}.$$
(A12)

Hence, inflation does not affect average output. To determine the impact on average capital and employment, notice from (6) and (7) and the fact that the productivity threshold is not affected by inflation that

$$d\ln\bar{n} = -(1-\nu)\sigma d\ln w - \nu\sigma d\ln r, \tag{A13}$$

$$d\ln \bar{k} = -\alpha\sigma d\ln w - (1-\alpha)\sigma d\ln r.$$
(A14)

Given that

$$\alpha d \ln w = -\nu d \ln r,\tag{A15}$$

from equation (21) and the fact that s^* is not affected by inflation, this set of equations can be rewritten as

$$d\ln\bar{n} = \frac{\nu}{\alpha} d\ln r,\tag{A16}$$

$$d\ln\bar{k} = -d\ln r. \tag{A17}$$

Thus, an increase in inflation increases the average level of employment per establishment, while it decreases average capital use. Equation (A9) is still valid if the CIA constraint only applies to investment. Consequently, if inflation increases average employment, decreases the wage rate and average capital, and does not affect average output and the productivity threshold, then it decreases the mass of incumbent establishments from equation (A9). Hence, aggregate output and stock of capital decrease too. But, the effect on aggregate employment is *a priori* ambiguous given that *H* decreases and \bar{n} increases. To show that the effect on aggregate employment is actually negative, first notice that

$$d\ln N = d\ln\bar{n} + d\ln H. \tag{A18}$$

Next, from equation (A9), observe that

$$d\ln H = d\ln w - Nd\ln w - Nd\ln \bar{n} + \frac{\delta KA\left(1 + \theta_c \left(\frac{1+g}{\beta} - 1\right)\right)}{w} d\ln \bar{k}.$$
(A19)

Replacing the above equation and (A15) and (A16) in (A19)

$$d\ln N = \frac{\delta K A \left(1 + \theta_c \left(\frac{1+g}{\beta} - 1\right)\right)}{w} d\ln \bar{k}.$$
 (A20)

Thus, aggregate employment decreases following an increase in inflation.

Case where $\theta_c = 0$, $\theta_k = 0$, and $\theta_h = 1$. Here the rental cost of capital is not affected by inflation (see equation (19)). To understand the effect on the productivity threshold and the wage rate, combine (8) and (21) with (20) to get

$$\kappa \left[1 + \theta_h \left(\frac{1+g}{\beta} - 1 \right) \right] = \left[1 - F(s^*) \right] \frac{\beta}{1 - \beta(1-\lambda)} \eta \left[\left(\frac{\bar{s}}{s^*} \right)^\sigma - 1 \right].$$
(A21)

Hence, an increase in inflation decreases the productivity threshold s^* . From equation (21) it follows that the wage rate decreases too. From (A12), average output either increases or remains unchanged, given that

$$d\ln\bar{y} = \sigma[d\ln\bar{s} - d\ln s^*],\tag{A22}$$

and $d \ln s^* \le d \ln \bar{s}$. To determine the effect on average employment and capital, notice from (21) that

$$d\ln s^{\star} = \alpha d\ln w. \tag{A23}$$

By replacing the above equation in (6) and (7), we have

$$d\ln\bar{n} = \sigma \left[d\ln\bar{s} - \frac{1-\nu}{\alpha} d\ln s^{\star} \right], \tag{A24}$$

$$d\ln\bar{k} = \sigma[d\ln\bar{s} - d\ln s^*]. \tag{A25}$$

Hence, average capital increases or remains unchanged following an increase in the rate of money growth and the impact of inflation on average employment is ambiguous. We now investigate the effect of g on H. Observe that we have from (A9) that

$$d\ln H = d\ln w - \frac{AY}{w} d\ln \bar{y} + \frac{AX}{w} d\ln \bar{k} - Nd\ln w - Nd\ln \bar{n} + \frac{AE\kappa}{w} \frac{f(s^*)s^*}{1 - F(s^*)} d\ln s^*.$$
(A26)

The above equation can be rewritten as

$$d\ln H = \left\{\frac{AX\sigma}{w} - \frac{AY\sigma}{w} - N\sigma\right\} d\ln \bar{s} + \left\{\frac{1-N}{\alpha} + \frac{N\sigma(1-\nu)}{\alpha} + \frac{AY\sigma}{w} - \frac{AX\sigma}{w} + \frac{AE\kappa}{w}\frac{f(s^{\star})s^{\star}}{1-F(s^{\star})}\right\} d\ln s^{\star}.$$

Given $d \ln \bar{s} \le d \ln s^*$, $Y \ge X$, and $(1 - N)/\alpha + N\sigma(1 - \nu)/\alpha > N\sigma$, it follows the mass of incumbents *H* decreases as a result of an increase in *g*. The impact on aggregate employment is given by

$$d\ln N = \left\{ \frac{AX\sigma}{w} - \frac{AY\sigma}{w} + (1-N)\sigma \right\} d\ln \bar{s} + \left\{ \frac{AY\sigma}{w} - \frac{AX\sigma}{w} + \frac{AE\kappa}{w} \frac{f(s^*)s^*}{1 - F(s^*)} - (1-N)\sigma \right\} d\ln s^*.$$

By use of (14) and (18), this equation simplifies as

$$d\ln N = \left\{ \frac{AC\sigma}{w} \theta_c \left(\frac{1+g}{\beta} - 1 \right) - \frac{AE\kappa\sigma}{w} \right\} d\ln \bar{s} + \left\{ \frac{AE\kappa}{w} \frac{f(s^*)s^*}{1 - F(s^*)} - \frac{AC\sigma}{w} \theta_c \left(\frac{1+g}{\beta} - 1 \right) + \frac{AE\kappa\sigma}{w} \right\} d\ln s^*.$$

Hence, aggregate employment decreases following an increase in g if $\theta_c = 0$. Notice that, from (A22) and (A25), the effect on average capital and average output is the same. Hence, to determine the effect on aggregate output and capital, it is sufficient to

know only one of the two effects given that they are the same. We choose to determine the effect on aggregate output:

$$d\ln Y = d\ln \bar{y} + d\ln H. \tag{A27}$$

This equation can be rewritten as

$$d\ln Y = \left\{\frac{AX\sigma}{w} - \frac{AY\sigma}{w} + (1-N)\sigma\right\} d\ln \bar{s} + \left\{\frac{AY\sigma}{w} - \frac{AX\sigma}{w} + \frac{AE\kappa}{w}\frac{f(s^*)s^*}{1 - F(s^*)} - (1-N)\sigma + \frac{1}{\alpha}\right\} d\ln s^*.$$

Given the discussion regarding the effect of g on N, by the same arguments, it follows that the effect of g on Y and K is negative as well.

A.4 Household Optimal Behavior

The Bellman equation characterizing household's optimal behavior reads as

$$V(m_{t-1}, K_t, H_t) = \max_{C_t, L_t, m_t, K_{t+1}, H_{t+1}} \{ \ln C_t + A \ln L_t + \beta V(m_t, K_{t+1}, H_{t+1}) \},$$
(A28)

and is subject to the CIA constraint (1) and the budget constraint (3). Let ϕ_t and γ_t be the Kuhn–Tucker multipliers for the constraints (1) and (3), respectively. The first-order conditions which characterize the solution to the problem of the household are

$$\frac{1}{C_t} - \theta_c \phi_t - \gamma_t = 0, \tag{A29}$$

$$\frac{A}{L_t} - \gamma_t w_t = 0, \tag{A30}$$

$$\beta V_1(m_t, K_{t+1}, H_{t+1}) - \frac{\gamma_t}{p_t} = 0, \tag{A31}$$

$$\beta V_2(m_t, K_{t+1}, H_{t+1}) - \theta_k \phi_t - \gamma_t = 0, \tag{A32}$$

$$\beta V_3(m_t, K_{t+1}, H_{t+1}) - \kappa(\theta_h \phi_t + \gamma_t) = 0,$$
(A33)

plus the budget constraint and the complementary slackness condition associated with the budget constraint. Moreover, by the envelope theorem, the shadow values of money, capital, and the mass of establishments are, respectively,

$$V_1(m_{t-1}, K_t, H_t) = \frac{\phi_t + \gamma_t}{p_t},$$
(A34)

$$V_2(m_{t-1}, K_t, H_t) = (1 - \delta)(\theta_k \phi_t + \gamma_t) + \gamma_t r_t,$$
(A35)

$$V_3(m_{t-1}, K_t, H_t) = (1 - \lambda) \kappa \left(\theta_h \phi_t + \gamma_t\right) + \gamma_t \left[1 - F(s_t^*)\right] \bar{z}_t.$$
(A36)

Combining (A34), (A35), and (A36) and the first-order conditions (A31), (A32), and (A33) yields the three Euler equations

$$\beta \frac{\phi_{t+1} + \gamma_{t+1}}{p_{t+1}} - \frac{\gamma_t}{p_t} = 0, \tag{A37}$$

$$\beta (1-\delta) (\theta_k \phi_{t+1} + \gamma_{t+1}) + \beta \gamma_{t+1} r_{t+1} - \theta_k \phi_t - \gamma_t = 0, \tag{A38}$$

$$\beta (1-\lambda) \kappa \left(\theta_h \phi_{t+1} + \gamma_{t+1}\right) + \beta \gamma_{t+1} \left[1 - F(s_{t+1}^{\star})\right] \bar{z}_{t+1} - \kappa \left(\theta_k \phi_t + \gamma_t\right) = 0.$$
(A39)

Equations (A29) and (A37)–(A39), combined with the intratemporal first-order condition (A30), the CIA constraint (1), and the budget constraint (3) characterize the solution to the household problem.

A.5 Optimal Monetary Policy

Here we derive the optimal rate of inflation. The proof relies on the observation that the optimal inflation rate corresponds to the case where the CIA constraint is not binding. When the CIA constraint is not binding the corresponding Lagrange multiplier is zero—i.e., $\phi_t = 0$ for all *t*. To derive the optimal rate of inflation we start by noticing that equation (A37) can be rewritten as

$$\phi_{t+1} = \frac{\gamma_t}{\beta} \frac{p_{t+1}}{p_t} - \gamma_{t+1}.$$
(A40)

Hence, $\phi_{t+1} = 0$ if and only if

$$\frac{\gamma_{t+1}}{\gamma_t} = \frac{p_{t+1}/p_t}{\beta}.$$
(A41)

Given that γ_t is constant in the stationary equilibrium and positive (from equation (A30)), and the growth rate of money is equal to inflation in that equilibrium, it follows that the Friedman rule applies to the stationary equilibrium of our model, that is, the optimal rate of inflation is equal to $(\beta - 1)$.

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